

### STUDENT COMPANION NSW

	120 <sup>1</sup> 150 <sup>1</sup>
	90 km/h
Pearson   Secondary Teaching Hub	



# Pearson Seconda Teach Maths SW **Student Companion**

**Contributing authors:** 

Greg Carroll, David Coffey, Grace Jefferson, Daine Oliver, Shaun Oliver, Sarah Plummer, Nicola Silva

Pearson acknowledges the Traditional Custodians of the lands upon which the many schools throughout Australia are located.

We respect the living cultures of Aboriginal and Torres Strait Islander peoples and their ongoing connection to Country across lands, sky, seas, waterways and communities. We celebrate the richness of Indigenous Knowledge systems, shared with us and with schools Australia-wide.

We pay our respects to Elders, past and present.

#### Pearson Australia

(a division of Pearson Australia Group Pty Ltd) 459–471 Church Street Level 1, Building B Richmond, Victoria 3121 www.pearson.com.au Copyright © Pearson Australia 2023 (a division of Pearson Australia Group Pty Ltd) First published 2023 by Pearson Australia 2026 2025 2024 2023

10 9 8 7 6 5 4 3 2 1

#### Reproduction and communication for educational purposes

The Australian Copyright Act 1968 (the Act) allows a maximum of one chapter or 10% of the pages of this work, whichever is the greater, to be reproduced and/or communicated by any educational institution for its educational purposes provided that that educational institution (or the body that administers it) has given a remuneration notice to the Copyright Agency under the Act. For details of the copyright licence for educational institutions contact the Copyright Agency (www. copyright.com.au).

#### Reproduction and communication for other purposes

Except as permitted under the Act (for example any fair dealing for the purposes of study, research, criticism or review), no part of this book may be reproduced, stored in a retrieval system, communicated or transmitted in any form or by any means without prior written permission. All enquiries should be made to the publisher at the address above. This book is not to be treated as a blackline master; that is, any photocopying beyond fair dealing requires prior written permission.

Project Leads: Natalie Bennett, Julian Lumb, Jack Sagar, Sarah Suess Development Editor: Schools Programme Manager: Michelle Thomas Production Editors: Maddy Higginson, Jaimir Kuster Editor: Designer: Rights & Permissions Editor: Amirah Fatin Binte Mohamed Sapi'ee Illustrators: DiacriTech and QBS Learning Proofreader: Printed in Australia ISBN 9780655713821 Pearson Australia Group Pty Ltd ABN 40 004 245 943

#### Disclaimer

Any internet addresses (URLs) provided for this Student Companion were valid at the time of publication and were chosen as being appropriate for use as a secondary education research tool. However, due to the dynamic nature of the internet, some addresses may have changed, may have ceased to exist since publication, or may inadvertently link to sites with content that could be considered offensive or inappropriate. While the authors and publisher regret any inconvenience this may cause readers, no responsibility for any such changes or unforeseeable errors can be accepted by either Pearson Australia or the authors.

### Contents

• • • • • •	• • • • • • • • • • • • • • • • • • • •		
1	<b>Computation with integers</b>	Χ	3
	Understand integers and operations	Х	
	Add and subtract integers	Х	
	Model and solve practical problems using integers	Х	
	Multiply and divide integers	Х	
	Solve problems by multiplying and dividing integers	х	
	Using the four operations with integers	sХ	
2	Understanding fractions and decimals	X	
	Understand and create equivalent fractions	х	
	The lowest common denominator and comparing fractions	х	4
	Simplify fractions	Х	
	Understand how to add and subtract fractions	х	
	Understand mixed numbers and improper fractions	x	
	Calculate the fraction of an amount	X	
	Understand how to multiply fractions	Х	
	Understand how to divide fractions	Х	
	Locate fractions and decimals on a number line	х	
	Compare fractions and decimals on a number line	х	
	Rounding decimals for different purposes	х	
	Add and subtract decimals	Х	
	Understand how to multiply decimals	Х	
	Understand how to divide decimals	Х	
	Identify and use irrational numbers	Х	
	Identify the golden ratio and make the connection between the circumference and diameter of any		
	circle	Х	
	Identify and use terminating, recurring and non-recurring decimals	х	

3	Algebraic techniques	X
	Understand variables in algebra	Х
	Identify and simplify like terms	Х
	Calculate the value of algebraic expressions	Х
	Write algebraic expressions in context	Х
	Understand and use the distributive law to expand simple algebraic expressions	x
	Factorise simple algebraic expressions	x
	Simplify algebraic expressions involving multiple operations	Х
•••••		• • ••
4	Understanding percentages	X
0	Understand the relationship between decimals, percentages and fractions	Х
X	Choose an appropriate representation to solve problems	Х
	Determine the proportion of a quantity	Х
	Understand percentage as applied to taxation	х
	Use fractions, decimals and percentages to solve financial	v
	problems	X X
	Percentage discounts and mark-ups	X
	Understand percentage increase and decrease	Х
	Understand percentage changes in practical situations	х

### Contents

#### **Equations** 5

. . . . . . . . . .

Indices	x
Solve simple quadratic equations	X
Understand solutions to simple quadratic equations	Х
Use a balance method to solve linear equations	Х
Use flowcharts to solve linear equations	Х
Use flowcharts to determine the value of an expression	Х
Write linear equations to represent diagrams and patterns	Х
Write linear equations to represent simple word problems	Х

Х

6 Indices

.....

marces	~
Understand and calculate squares and square roots	Х
Understand and calculate cubes and cube roots	x
Understand and use index notation to represent numbers	x
Represent numbers in prime factor form	x
Understand and identify common factors	х
Understand and use expanded notation to represent numbers	х
Establish and apply the index law for multiplication	х
Establish and apply the index law for division	х
Establish and apply the index law for raising a power to a power	
Establish and apply the index law for raising to the power of zero	Х

7	Length and perimeter	Χ
	Estimate length and convert between units of length	Х
	Calculate the perimeter of quadrilaterals	х
	Determine unknown side lengths from a given perimeter	х
		• • • ••
8	Areas of triangles and quadrilaterals	X
	Understand and convert area units	Х
	Calculate areas of rectangles	Х
	Calculate the areas of parallelograms and rhombuses	х
	Calculate areas of triangles	Х
	Calculate areas of trapeziums	Х
	Calculate areas of kites and rhombuses	х
9	Angle relationships	Χ

**Angle relationships** 

Use angles terminology and symbols Х Determine the size of angles at a point X Determine the size of angles with transversals on parallel lines Х

10	Data Classification	X
	Understand different data types	Х
	Classify categorical data as ordinal or nominal	Х
	Construct and interpret pictograms	Х
	Construct and interpret column graphs	Х
	Construct and interpret divided bar graphs and sector graphs	Х
	Understand stem-and-leaf plots	Х
	Create and interpret statistical plots	Х
	Interpret line graphs and histograms	Х
	Construct line graphs, histograms and polygons	Х
	Choose appropriate data representations	

### How to use this Student Companion

The Student Companion is a complementary resource that offers a print medium for corresponding lessons in Pearson Secondary Teaching Hub. It is designed to support teaching and learning by providing learners with a place to create a portfolio of learning to suit their individual needs, whether you are:

- supporting a blended classroom using the strengths of print and digital
- preparing for exams by creating a study guide or bound reference
- needing a tool to differentiate learning or
- looking for meaningful homework tasks.

Learners can develop their portfolio of learning as part of classroom learning or at home as an additional opportunity to engage and re-engage with the knowledge and skills from the lesson.

This could be done as prior learning in a flipped classroom environment or as an additional revision or homework task.

#### Learning intention and success criteria

#### Understand and calculate squares and square roots

• Learning intention: To be able to recognise circle features and understand the relationship between the radius and the diameter of a circle.

- SC 1: I can identify square numbers.
- SC 2: I can determine the square root of a square number.
- SC 3: I can place the square root of any number between its two closest natural numbers.
- SC 4: I can apply squares and square roots to real-life situations.

SC 1: I can identify square numbers

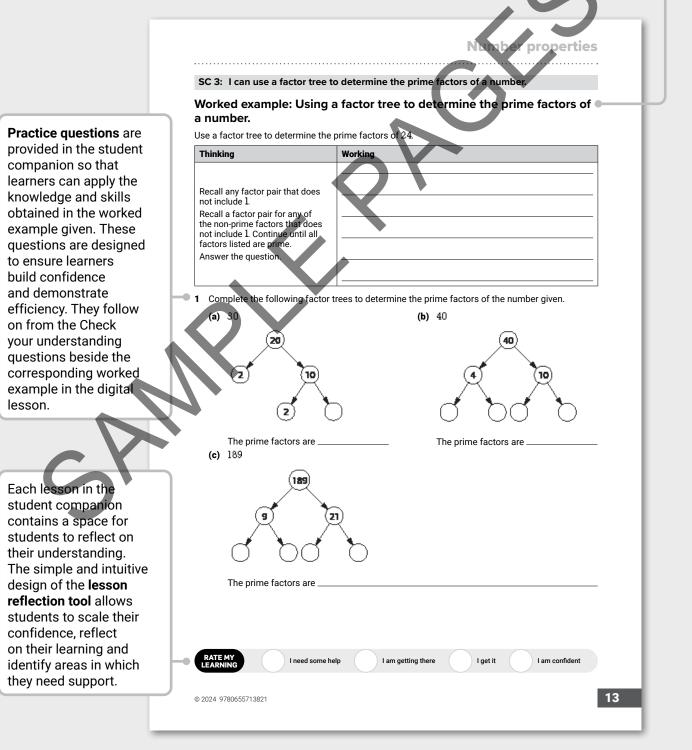
**Learning intentions** are provided for every lesson. The learning intentions are goals or objectives that align to the corresponding digital lesson. They describe what learners should know, understand or be able to do by the end of the lesson. **Success criteria** clarify expectations and describe what success looks like. The success criteria are specific, concrete and measurable so learners can actively engage with and reflect on their evidence of learning within each lesson.

#### **Worked examples**

Worked examples provide learners with a step-by-step solution to a problem. The worked examples in the Student Companion correspond to those in the digital lesson and are provided for each skill to:

- scaffold learning
- support skill acquisition
- reduce the cognitive load.

The **worked examples** are an effective tool to demonstrate what success looks like. The 'try yourself' format of the worked examples in the Student Companion support the gradual release of responsibility. Learners can view a completed worked example and a video walkthrough of the worked example in the corresponding digital lesson and then apply the scaffolded steps themselves to solve a unique problem.



### **Number properties**

#### Understand and calculate squares and square roots

**Learning intention:** To be able to recognise circle features and understand the relationship between the radius and the diameter of a circle.

- SC 1: I can identify square numbers.
  - SC 2: I can determine the square root of a square number.
  - SC 3: I can place the square root of any number between its two closest natural numbers.
- SC 4: I can apply squares and square roots to real-life situations.

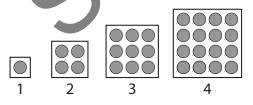
#### SC 1: I can identify square numbers

#### Worked example: Identifying common square numbers

(a) Is 16 a square number?

	Thinking	Working	
	Recall the factors of 16. Can 16 be written as the product of a number multiplied by itself?		
	Write the answer.		
(b)	ls 8 a square number?		
	Thinking	Working	
	Recall the factors of 8. Can 8 be written as the product of a number multiplied by itself?		
	Write the answer.		

1 Some square numbers are represented by counters in the diagrams below.



(a) The diagrams show the first four square numbers 1, 4, 9 and 16. Explain what these numbers represent.

### **Number properties**

- (b) How many counters would you need to make the fifth square number?
- (c) You can also create squares with arrays On the grid below, draw squares with sides 5 units and 6 units.

- (d) Determine the area of the squares you drew in part (c).
- (e) Explain how you would calculate the value of a square number.
- (f) How would you work out the area of a square with side lengths of 8 units?
- 2 Complete this table of the first 20 square numbers.

$1^2 = 1$ $6^2 =$	
$2^2 = 4$	
$3^2 = 9$	
$4^2 \equiv$	
$5^2 =$	

**3** Which of the following numbers are square numbers? Justify your answer.



#### SC 2: I can determine the square root of a square number

#### Worked example: Calculating the square root of a square number

Determine the square root of the square number 36.

٦	hink	ing		Working
t it	nat w	hen mu gives th	e number Iltiplied by Ie square	
V	Vrite	the ans	wer.	
1	Det	ermine	the square r	oot of the following square numbers.
	(a)	9		
	(b)	49		
	(c)	64		
	(d)	121		
	(e)	196		
	( <b>f</b> )	225		
2			As the squar o's mistake.	e root of 4 is 2. Then the square root of 16 is 8".
		Ç	2	

### SC 3: I can place the square root of any number between its two closest natural numbers

#### Worked example: Estimating the value of the square root of a number

. . . . . . . . . . . .

The square root of 60 is between which two whole numbers?

Thinking	Working
Recall the square numbers above and below 60.	
Write the square root for each number.	
Write the answer.	
<b>1</b> The square root of 20 is	s between which two whole numbers?
	umber above and below the square root of:
(a) 12	
<b>(b)</b> 40	
(c) 115	
(d) 300	
3 Place the following squ	are roots on the number line shown.
( <b>a</b> ) √6	(b) $\sqrt{18}$ (c) $\sqrt{77}$ (d) $\sqrt{250}$
	6 7 8 9 10 11 12 13 14 15 16 17 18 19 20
RATE MY LEARNING	ed some help I am getting there I get it I am confident
	pearson.com.au/teaching-hub

#### SC 4: I can apply squares and square roots to real-life situations

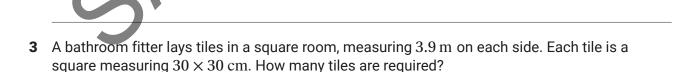
#### Worked example: Applying squares and square roots

A bathroom fitter will place tiles on a square section of wall. The square measures 2 m on each side. Each tile is a square measuring  $20 \times 20$  cm. How many tiles are required?

Thinking	Working
Calculate the number of tiles along one edge of the square.	
Since the section of wall is square, the number of tiles is found by squaring 10.	
Write the answer.	

1 A carpet fitter is laying square carpet tiles in a room. The room has a floor that is a square with sides 5 m. Each floor tile is  $50 \times 50 \text{ cm}$ . How many carpet tiles are required?

2 A bathroom fitter lays tiles on a square section of floor. The square measures 3 m on each side. Each tile is a square measuring  $20 \times 20 \text{ cm}$ . How many tiles are required?



RATE MY LEARNING	I need some help	I am getting there	I get it	I am confident	

### Understand and use index notation to represent numbers

Learning intention: To understand and be able to use index notation to represent numbers

SC 1: I can correctly use the terms 'base' and 'index'.

SC 2: I can express repeated multiplication by using index notation.

#### SC 1: I can correctly use the terms 'base' and 'index'.

#### Worked example: Identifying the base and index

Ide	entify the base and index in $5^{2}$	
Т	hinking	Working
T	lentify the base. he base is the large number t the bottom.	
T	dentify the index. he index (or power) is the uperscripted number.	
1	Identify the base and index in	17 <sup>3</sup> .
2	Identify the base and index in	n:
	(a) 3 <sup>2</sup>	
	<b>(b)</b> 4 <sup>5</sup>	
	(c) x <sup>4</sup>	
	(d) $m^n$	
3		of expressions written in index form.
	For example, $2^6 = x$ . Since $2^6 = 2 \times 2 \times 2 \times 2 \times 2$	$x \times 2 = 64, x = 64.$
	Calculate the value of $x$ in the	
	(a) $2^4 = x$	
	<b>(b)</b> $3^2 = x$	
	(c) $3^3 = x$	
	(a) $5 \equiv x$	
	RATE MY	
L	EARNING	

#### SC 2: I can express repeated multiplication by using index notation

## Worked example: Understanding the link between index and expanded form.

Write the expression  $9 \times 9 \times 9 \times 9$  in index form.

T	hinking	Working
l	dentify the base.	
c ti	dentify the index by ounting the number of mes the base occurs in he expression.	
V	Vrite the answer.	
1	Write the following in ir	ndext form.
	(a) $5 \times 5 \times 5 \times 5 \times 5$	×5
	(b) $5 \times 5 \times 5 \times 5 \times 5$	
	(c) $5 \times 5 \times 5 \times 5$	
	(d) $5 \times 5 \times 5$	
	(e) 5 × 5	
2	Write the following exp	ressions in index form.
	(a) $8 \times 8 \times 8 \times 8$	
	(b) $4 \times 4 \times 4 \times 4$	
	(c) $20 \times 20 \times 20 \times 20$	
	(d) $z \times z \times z \times z$	
3		brs are involved, they can be simplified by writing them in index form. $\times 5 \times 5 = 2^2 \times 5^3$ . Write the following expressions in index form.
	(a) $3 \times 3 \times 3 \times 5 \times 5$	
	(b) $4 \times 4 \times 7 \times 7 \times 7$	× 7
	(c) $3 \times 3 \times 3 \times 3 \times 3$	×11×11×11
	(d) $3 \times 3 \times 5 \times 5 \times 5$	×5×7×7×7

RATE MY LEARNING

### Represent numbers in prime factor form

Learning intention: To be able to represent numbers in prime factor form

- SC 1: I can determine the prime factors of a number
  - SC 2: I can use a factor ladder to find determine the prime factors of a number
- SC 3: I can use a factor tree to determine the prime factors of a number
- SC 4: I can write a number as a product of its prime factors

#### SC 1: I can determine the prime factors of a number

#### Worked example: Determine the prime factors of 24

Determine the prime factors of 24.

Thinking	Working
Write the first factor pair as a product of 1 and itself.	
Try 2, 3, 4, 5, 6 until there is no difference between the two factors, or the factors start repeating.	
List the factors.	
Highlight the factors that are prime numbers.	
Write the answer.	
(a) 8 (b) 20	
(c) 100	
RATE MY	I am getting there

5

LEARNING

#### SC 2: I can use a factor ladder to find determine the prime factors of a number.

## Worked example: Using a factor ladder to determine the prime factors of a number.

(a) Determine the prime factors of 18 using a factor ladder.

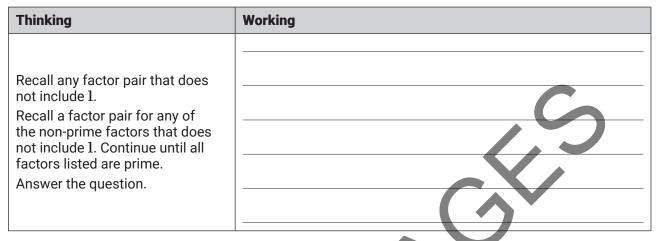
	Thinking	Working
	Recall the smallest prime number.	
	Divide the number by the smallest prime number until it no longer divides evenly or until the final division gives a result of 1.	
	Recall the next prime number.	
	Divide the result in the ladder by the next prime number until it no longer divides evenly or until the final division gives a result of 1.	
	Answer the question.	
<b>(b)</b>	Determine the prime factors of $24\iota$	using a factor ladder.
	Thinking	Working
	Recall the smallest prime number.	
	Divide the number by the smallest prime number until it no longer divides evenly or until the final division gives a result of 1.	
	Recall the next prime number.	
	Divide the result in the ladder by the next prime number until it no longer divides evenly or until the final division gives a result of 1. Try dividing by the next prime number 3.	
	Answer the question.	

- **1** Use a factor ladder to determine the prime factors of:
  - (a) 8 (b) 20 (c) 100

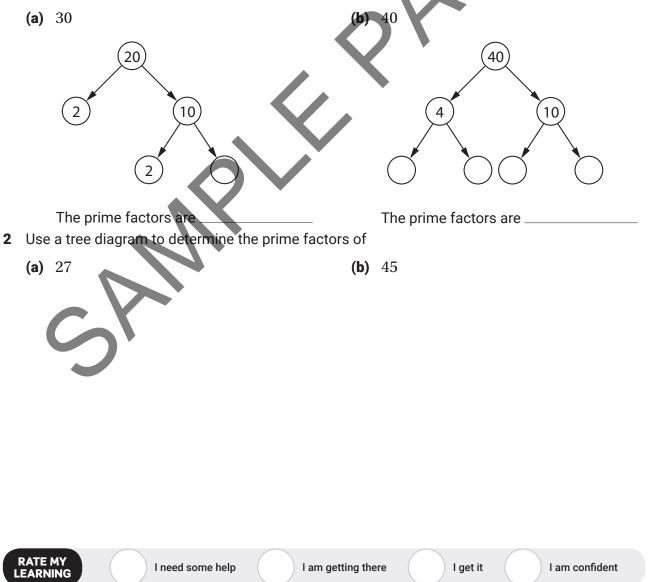
SC 3: I can use a factor tree to determine the prime factors of a number.

## Worked example: Using a factor tree to determine the prime factors of a number.

Use a factor tree to determine the prime factors of 24.



1 Complete the following factor trees to determine the prime factors of the number given.



#### SC 4: I can write a number as a product of its prime factors

## Worked example: Writing the prime factorisation of a number in index form

Write 92 as a product of its prime factors. Express your answer in index form.

Thinking		Working	
Use a factor ladde determine the prin			
Write the prime fa product.	ctors as a		
Express your answ form.	ver in index		
1 Express the fol form.	lowing numbers	as a product of their prime factors, then write them in index	
<b>(a)</b> 27			
<b>(b)</b> 20	(b) 20		
(c) 18	(c) 18		
( <b>d</b> ) 36			
(e) 225			
		he prime factors of 8 as $2 \times 2 \times 2$ . Noah then tried to simplify as $8 = 2 \times 3$ . What mistake has Noah made?	
6			
3 Answer true or	false for each of	the statements below.	
(a) The factor	s of 11 are 1 and	11	
(b) The prime	factors of 11 are	e 1 and 11.	
(c) The prime	factors of 10 are	2 and 5.	
(d) 44 written	as a product of i	its prime factors is $2 \times 2 \times 11$ .	

### Understand and identify common factors

Learning intention: To understand and be able to identify common factors

- SC 1: I can determine the highest common factor (HCF) of a pair of numbers.
- SC 2: I can determine the lowest common multiple (LCM) of a pair of numbers.
- SC 3: I can solve problems involving highest common factors and lowest common multiples.

#### SC 1: I can determine the highest common factor (HCF) of a pair of numbers

#### Worked example: Finding the highest common factor (HCF)

Determine the highest common factor (HCF) of 36 and 42.

Т	hinki	ng	Working
L	ist th	e factors of each number.	
tł U	ne fao se th	he lists of factors, identify ctors common to both lists. is list to identify the highest on factor (HCF)	
A	nswe	er the question.	
1	Dete	ermine the highest common	n factor (HCF) of 16 and 24.
	(a)	List the factors of 18.	
	(b)	List the factors of 24.	
	(c)	List the common factors of	of 16 and 24.
	(d)	Identify the highest commo	on factor (HCF).
2	Det	ermine the highest common	n factor (HCF) of 33 and 63.
	(a)	List the factors of 33.	
	(b)	List the factors of 63.	
	(c)	List the common factors of	of 33 and 63.
	(d)	Identify the highest commo	on factor (HCF).
	RATE	MY I need some hel	elp I am getting there I get it I am confident

LEARNING

#### SC 2: I can determine the lowest common multiple (LCM) of a pair of numbers

#### Worked example: Finding the lowest common multiple (LCM)

Determine the lowest common multiple of 8 and 10.

٦	hinki	ing	Working
	ist th ach.	e first five multiples for	
t	he lov	the list of multiples, identify west multiple that is on to both lists.	, Co
A	nswe	er the question.	
1	Det	ermine the lowest common	multiple (LCM) of 12 and 15.
	(a)	List the first 5 multiples of	12.
	(b)	List the first 5 multiples of	15.
	(c)	Identify the lowest commo	n multiple (LCM).
2	Det	ermine the lowest common	multiple (LCM) of 4 and 7.
	(a)	List the first 8 multiples of	4.
	(b)	List the first 8 multiples of	7.
	(c)	Identify the lowest commo	n multiple (LCM).
3	Det	ermine the lowest common	multiple (LCM) of 6, 9 and 12.
	(a)	List the first 6 multiples of	6
	(b)	List the first 4 multiples of	9
	(c)	List the first 3 multiples of	12.
	(d)	Identify the lowest commo	n multiple (LCM).

### SC 3: I can solve problems involving highest common factors and lowest common multiples

## Worked example: Solving problems using the lowest common multiple (LCM)

Determine the smallest whole number which when divided by 2, 3, 4 and 9 leaves a remainder of 1 each time.

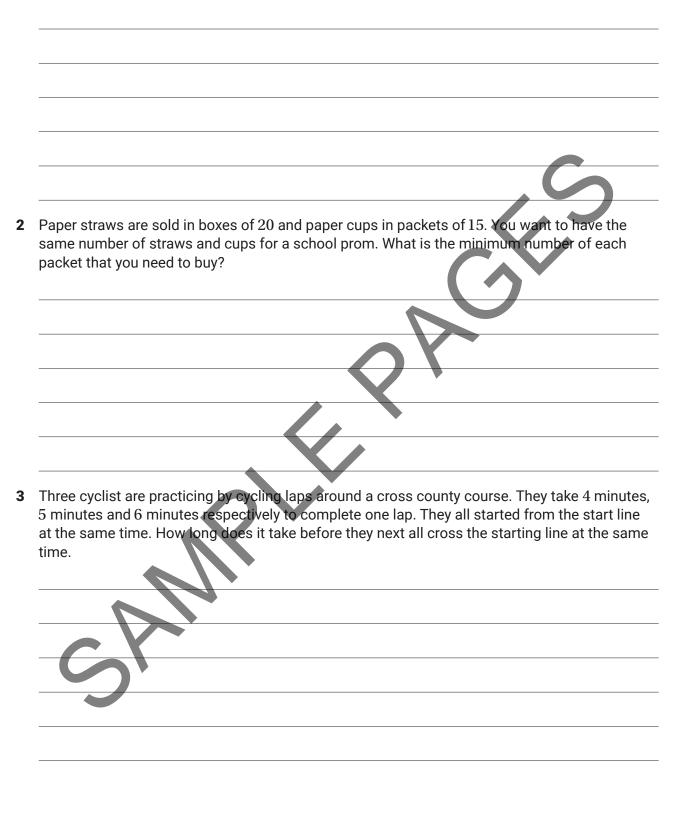
Thinking	Working
Describe the steps needed to solve the problem.	C
Determine the lowest common multiple of 2, 3, 4 and 9.	
Add 1 to the result.	
Check the reasonableness of your answer.	
Answer the question.	

## Worked example: Solving problems using the highest common factor (HCF)

An artist has 16 red tiles and 40 blue tiles. The tiles will be laid in rows containing the same number of red tiles and blue tiles, using all the tiles. How many rows will the artist need to create and how many of each tile will be in a row?

Thinking	Working
Describe the state based of to	
Describe the steps needed to solve the problem.	
List the factors of each number and identify the highest factor common to both lists	
Interpret the highest common factor (HCF).	
Determine the number of plants in each row.	
Write the answer.	

1 Four lights are set to flash at intervals of 5, 7, 10 and 14 seconds. If they all flash at 10am, when will they next all flash at the same time?



### Understand and use expanded notation to represent numbers

Learning intention: To understand and be able to use expanded notation to represent numbers

- SC 1: I can write large powers of ten in both expanded form and index form.
  - SC 2: I can write large numbers in expanded notation.

SC 1: I can write large powers of ten in both expanded form and index form

## Worked example: Writing large powers of 10 in expanded notation and index notation

(a) Write the number 1000 in both expanded form and index form.

Thinking	Working
Identify the base number.	
Write the number in expanded form. Expanded form shows the base number multiplied by itself	
Identify the number of times the base number appears in the product.	
Write the number in index form.	
The index shows the number of times the base number appears in the product. This is written as a superscript.	
Write the answer.	

(b) Write the number 1000000 in both expanded form and index form.

Thinking	Working
Identify the base number.	
Write the number in expanded form.	
Expanded form shows the base number multiplied by itself.	
Identify the number of times the base number appears in the product.	
Write the number in index form.	
The index shows the number of times the base number appears in the product. This is written as a superscript.	
Write the answer.	

- 1 Write the following in index form with a base of 10.
  - (a) 10000000 \_\_\_\_\_
    - **(b)** 10000000
    - (c) 100000000 \_\_\_\_

RATE MY EARNING

#### SC 2: I can write large numbers in expanded notation

#### Worked example: Writing in expanded form using powers of 10

Write 8057 in expanded form using index notation.

Thinking	Working
Write the number in expanded form.	
Rewrite the expanded form by multiplying each digit by a power of 10.	
Write each power of ten in index form.	
Recall that $1000 = 10^3$ , $100 = 10^2$ , $10 = 10^1$ and $10 = 10^0$ .	
Write the answer.	

1 Place value is shown in the table below. Complete the table with index numbers using 10 as a base.

	Hundreds of thousands	Tens of thousands	Tho <b>us</b> ands	Hundreds	Tens	Ones
General form	100000					
Index form			10 <sup>3</sup>		10 <sup>1</sup>	10 <sup>°</sup>
Expanded form		$10 \times 10 \times 10 \times 10$				1

**2** The number 879 is eight hundreds, seven tens and nine ones and can be written as  $(8 \times 100) + (7 \times 10) + (9 \times 1)$  or in expanded form using index notation as  $8 \times 10^2 + 7 \times 10^1 + 9 \times 10^0$ .

Write the following numbers in expanded form using index notation.

- **(a)** 37
- **(b)** 372
- (c) 3702
- **3** Write these numbers given in expanded notation in general form (as numbers).
  - (a)  $5 \times 10^2 + 3 \times 10^1 + 9 \times 1$
  - **(b)**  $7 \times 10^2 + 5 \times 1$
  - (c)  $2 \times 10^2 + 3 \times 10^0$

RATE MY EARNING